

III Semester M.C.A. Examination, April/May 2022 (CBCS)

COMPUTER SCIENCE MCA 304 : Statistical Analysis

Time: 3 Hours

Max Marks: 70

Instructions: 1) Answer all Sections.

2) Answer any five questions from Section - A and answer any four questions from Section - B.

SECTION - A

Answer any 5 questions. Each question carries 6 marks :

 $(5 \times 6 = 30)$

a) State and prove addition theorem of probability.

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b) Two fair dice are rolled at once. Find the probability that the sum of the numbers obtained is 7 or 10.

3

6

Find the unknown 'K' in the following probability distribution and also find E(X), Var(X) and SD(X)

X	0	1	2	3	4

3/8 3/16 1/16

State and prove Baye's theorem.

6

6

4. Calculate the coefficient of correlation between x and y for the following data:

х	21	22	23	24	25	26	27	28	29	30
у	11	12	13	14	15	16	17	18	19	20

5. Derive mean and variance of Poisson's distribution.

6

Fit an equation of the form y = ax^b to the following data:

6

Х	1	2	3	4	5
у	0.5	2	4.5	8	12.5



- The probabilities that a patient recovers from COVID-19 is 0.8. If 10 people are known to have contacted COVID-19, what is the probability that
 - i) 7 of them recover

ii) Atleast 9 of them recover.

6

From the following series of annual data, find the trend line by the method of semi-averages by plotting the trend line, also estimate the value of 2006.

6

Year	2000	2001	2002	2003	2004	2005
Annual values	170	231	261	267	278	302

SECTION - B

Answer any 4 questions. Each question carries 10 marks :

 $(4 \times 10 = 40)$

9. The joint probability distribution of X and Y are given below:

10

XY	1	2	3
1	0.186	0.148	0.074
2	0.037	0.111	0.111
3	0.111	0.148	0.074

Find:

- i) Marginal probability distribution of X and Y
- ii) E(X) and E(Y)
- iii) V(X) and V(Y)
- iv) Conditional distribution of Y given X = 1
- v) Conditional distribution of X when Y < 2.
- 10. a) Three machines M₁, M₂ and M₃ manufactures respectively 40%, 50% and 10% of total production. The percentage of defective items produced by M₁, M₂, M₃ are 2%, 4% and 5% respectively. If an item is chosen at random and is found to be defective. Find the probability that it is being a product of M₃.
 - b) Define simple random sampling and stratified random sampling with example.

11. Given the bivariate data:

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6

4

Х	1	5	3	2	1	1	7	3
у	6	1	0	0	1	2	1	5

- i) Fit the two regression lines (x on y and y on x)
- ii) Predict x if y = 2.5
- iii) Compute the correlation coefficient.

5

5

5

5

10



12. a) Calculate the coefficient of rank correlation from the following data:

Х	50	81	75	88	95	90	60	80
у	100	142	120	134	150	115	110	140

 b) The following are the values of production (in thousand meters) of a cloth mill.

Year	2002	2004	2006	2008	2010	2012	2014
Production	75	79	86	92	92	94	96

- i) Fit a straight line trend (y = a + bx) using least square method.
- ii) Estimate the production in the year 2016.
- 13. a) In order to test whether the attributes, COVID-19 infection and gender are independent, a survey of 80 people was conducted and the results are as given below. Conduct chi-square test for independence of attributes at 5% level of significance.

 COVID -Ve
 COVID +Ve

 Male
 20
 30

 Female
 8
 19

- b) The orange fruits grown in a large orchard have a mean weight of 19.3 ounces with a S.D. of 2.2 ounces. Assuming that the distribution of the weight of these orange fruits has the shape of normal distribution, find
 - i) what percentage of the orange fruits weigh less than 18 ounces.
 - ii) what percentage of the orange fruits weigh atleast 20 ounces.

14. A random sample of 5 truck tyres is taken from each of 3 brands manufactured by 3 companies. The life time of these tyres are given below. Use analysis of variance technique to determine whether the average life time of 3 brands of tyres are equal or not. Test 'α'at 5%.

Brand 1	35	34	34	33	34
Brand 2	32	32	31	28	29
Brand 3	34	33	32	32	33